

Example 1 – Here is a table from Augustus Gloop’s dad’s deal.

List out the number of candies that Augustus will get each day get as a sequence.

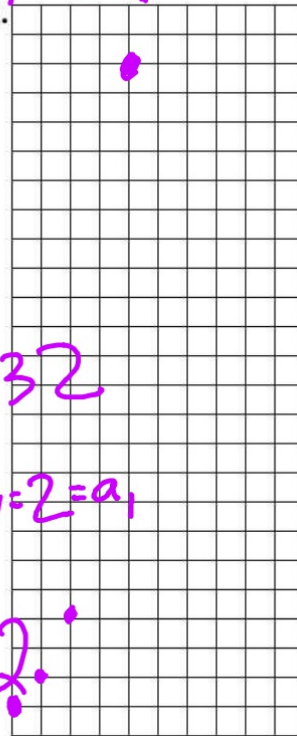
$\{1, 2, 4, 8, 16, 32, 64\}$

What do you do to calculate the number of candy received on the next day?

double
 $\times 2$

Day	Candies
a_0	1
a_1	2
a_2	4
a_3	8
a_4	16
a_5	32
a_6	64

Graph the sequence on the graphing grid.



Calculate the number of candies Augustus would get on day 25. How did you calculate it?

$f(x) = 2^x = 2^{25}$
3355432

Recursive Formulas –

$a_n = a_{n-1} \cdot 2, a_0 = 1$

$a_1 = a_{1-1} \cdot 2 = a_0 \cdot 2 = (1)(2) = 2 = a_1$

Explicit Formulas –

$f(n) = 1 \cdot 2^n$
 $f(1) = 1 \cdot 2^1 = 2$

Example 2 – Here is a table from Augustus Gloop’s mom’s deal.

List out the number of candies that Augustus will get each day get as a sequence.

$\{0, 20, 40, 60, 80, 100, 120\}$

What do you do to calculate the number of candy received on the next day?

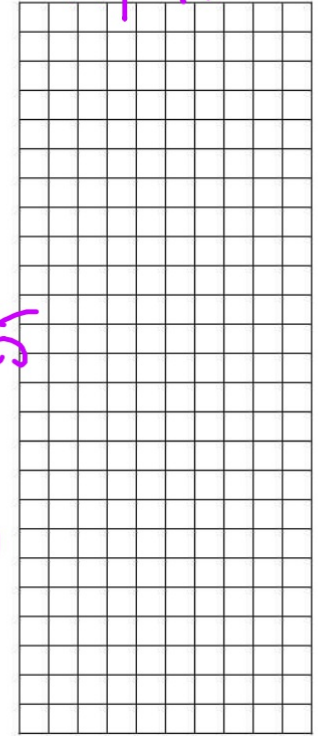
$f(x) = 20x$

Day	Candies
0	0
1	20
2	40
3	60
4	80
5	100
6	120

$7 \times 20 = 140$

Calculate the number of candies Augustus would get on day 25. How did you calculate it?

$f(n) = 20n$
 $n = 25$
 $f(n) = 20n$
 $f(25) = 20(25)$
500



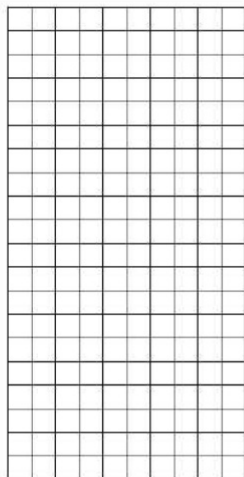
Example 3 – Complete the sequence by using recursion

$A = \{5, 9, 13, 17, a_5, a_6, 29, 33, 37, a_{10}\}$

What are the fifth, sixth, and tenth terms of the sequence?

$a_n = a_{n-1} + 4$
 $a_5 = a_{5-1} + 4$
 $a_5 = a_4 + 4 = 17 + 4 = 21$
 $a_6 = 25$
 $a_{10} = 41$

Graph the Sequence.



Example 4 – Find the missing terms in the sequence using recursion.

$B = \{6, 18, 54, 162, b_5, b_6, 4374, b_8\}$

What are the fifth, sixth, and tenth terms of the sequence?

$b_5 = b_{5-1} \cdot 3$
 $b_5 = b_4 \cdot 3 = 162(3)$
 $b_6 = 486$
 $b_8 = 13122$

Graph the Sequence.



Example 5 – What is the fourth term in the sequence given by $f(n) = 3n - 7$?

$f(4) = 3(4) - 7 = 12 - 7 = 5$

Example 6 – Write the first four terms of the following sequences.

A. $a_n = a_{n-1} - 5$; $a_0 = -3$ $a_1 = -8$ $a_2 = -13$ $a_3 = -18$ $a_4 = -23$

$a_1 = a_{1-1} - 5$ $a_2 = a_{2-1} - 5$

$a_1 = a_0 - 5$ $a_2 = a_1 - 5$

$a_1 = -3 - 5 = -8$ $a_2 = -8 - 5 = -13$

B. $a_n = -3[a_{n-1}]$; $a_0 = 2$ $a_1 = -6$ $a_2 = 18$ $a_3 = -54$ $a_4 = 162$

$a_1 = -3[a_{1-1}]$ $a_2 = -3[a_{2-1}]$ $a_3 = -3[a_{3-1}]$

$a_1 = -3(a_0) = -6$ $a_2 = -3(a_1)$ $a_3 = -3(a_2)$

C. $f(n) = 1200 \left(\frac{1}{4}\right)^n$ $f(1) = 300$ $f(2) = 75$ $f(3) = 18.75$ $f(4) = 4.6875$

Example 7 – Find the fifth term of a sequence when...

$a_n = 4[a_{n-1}]$; $a_3 = 25$ $a_4 = 100$ $a_5 = 400$

$a_4 = 4[a_{4-1}]$ $a_5 = 4[a_{5-1}]$

$a_4 = 4(a_3) = 4(25) = 100 = 4(a_4)$
 $4(100) = 400$

