

Vocabulary Words

Perimeter: Add all the sides together

Calculating Perimeter: 1. Use the distance formula to find each side length
2. Add all side lengths

Area: $A = b \cdot h$ or $A = l \cdot w$

Calculating Area of a Rectangle: 1. Use the distance formula to find each side length
2. Multiply the 2 sides that are different lengths

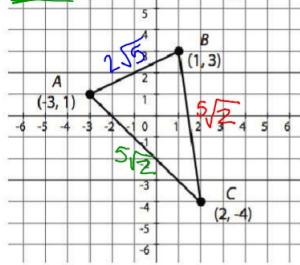
Example 1: Triangle ABC has vertices A(-3, 1), B(1, 3), and C(2, -4). Calculate the perimeter of the triangle.

$$\begin{aligned} AB &= \sqrt{(-3-1)^2 + (1-3)^2} \\ &= 2\sqrt{5} \end{aligned}$$

$$\begin{aligned} BC &= \sqrt{(1-2)^2 + (3-4)^2} \\ &= 5\sqrt{2} \end{aligned}$$

$$\begin{aligned} CA &= \sqrt{(2-(-3))^2 + (-4-1)^2} \\ &= 5\sqrt{2} \end{aligned}$$

$$2\sqrt{5} + 5\sqrt{2} + 5\sqrt{2} = \boxed{2\sqrt{5} + 10\sqrt{2} \text{ or } 18.6}$$



Example 2: Rectangle ABCD has vertices A(-3, -4), B(-1, 2), C(2, 1), and D(0, -5). Calculate the area and perimeter of the rectangle.

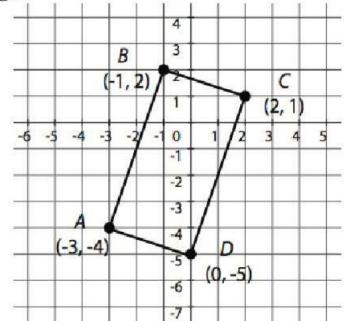
$$AB = \sqrt{(-3-(-1))^2 + (-4-2)^2} = 2\sqrt{10}$$

$$BC = \sqrt{(-1-2)^2 + (2-1)^2} = \sqrt{10}$$

$$CD = \sqrt{(2-0)^2 + (1-(-5))^2} = 2\sqrt{10}$$

$$DA = \sqrt{(0-(-3))^2 + (-5-4)^2} = \sqrt{10}$$

$$2\sqrt{10} \cdot \sqrt{10} = 20 \text{ units}$$



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| Sec1 | Notes 4-3 Applications of Distance Formula | Unit 4 |
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Definition of Circle: Made up of points that are the same distance from the center (Radius)

Example 3: Given this circle with an origin of the center and radius 5... $(0,0)$

A. Is $(4, 3)$ on the circle?

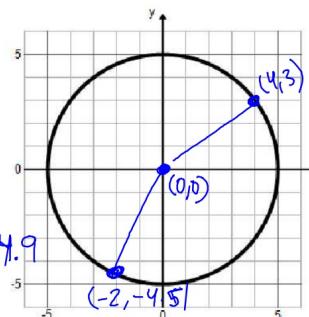
$$\sqrt{(4-0)^2 + (3-0)^2} = 5$$

Yes

B. Is $(-2, -4.5)$ on the circle?

$$\sqrt{(-2-0)^2 + (-4.5-0)^2} = 4.9$$

No



C. Is $(\sqrt{7}, 3\sqrt{2})$?

$$\sqrt{(\sqrt{7}-0)^2 + (3\sqrt{2}-0)^2} = 5$$

Yes

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Example 4: Given a circle with radius 4 and centered at $(1, 3)$: prove whether or not the following points are on the circle.

A. $(3.5, 6)$ and $(1, 3)$

$$\sqrt{(3.5-1)^2 + (6-3)^2} = 3.9$$

NO

B. $(1, 7)$ and $(1, 3)$

$$\sqrt{(1-1)^2 + (7-3)^2} = 4$$

Yes

