

Sec1H

Notes 4-4
Function Operations

Unit 4

Warm Up-

1. Evaluate the function $f(x) = x^2 - 9$ given the inputs $\{-4, 0, 2, 4\}$.

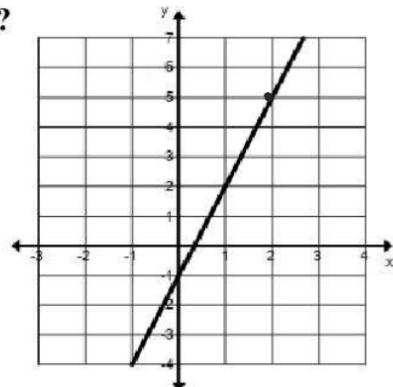
$$f(-4) = (-4)^2 - 9 = 7$$

$$f(0) = (0)^2 - 9 = -9$$

$$\{7, -9, -5, 7\}$$

2. Given the graph, what is $f(2)$?

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3. Given the table, what is $f(0)$?

7

| x | $f(x)$ |
|-----|--------|
| 0 | 7 |
| 1 | 5 |
| 2 | 3 |
| 3 | 1 |
| 4 | 0 |

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Operations of Functions

| Operation | Notation | Ex: $f(x) = 6x, g(x) = 3x + 2$ | Does Order Matter? |
|-------------|---------------|---------------------------------|---------------------------------|
| Addition | $(f+g)(x)$ | $(f+g)(x)$ $= 6x + 3x + 2$ | $(g+f)(x)$ $= 3x + 2 + 6x$ |
| | $f(x) + g(x)$ | $= 9x + 2$ | $= 9x + 2$ |
| Subtraction | $(f-g)(x)$ | $(f-g)(x)$ $= 6x - (3x + 2)$ | $(g-f)(x)$ $= 3x + 2 - (6x)$ |
| | $f(x) - g(x)$ | $= 6x - 3x - 2$ $= 3x - 2$ | $= -3x + 2$ |

Example 1: Let $f(x) = x - 8$ and $g(x) = 2x + 3$

A. $(f + g)(x) =$

$$3x - 5$$

B. $(g - f)(x) =$

$$2x + 3 - (x - 8)$$

$$2x + 3 - x + 8$$

$$x + 11$$

C. $(f - g)(x) = x - 8 - (2x + 3)$

$$-x - 11$$

~~ANOTHER~~

$$x - 8 - 2x - 3$$

$$-x - 11$$

$$-(x + 11)$$

D. $(f + g)(x) - 6 =$

$$3x - 5 - 6$$

$$3x - 11$$

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| <i>Operation</i> | <i>Notation</i> | <i>Example:</i> $f(x) = 6x, g(x) = 3x + 2$ | <i>Does order matter?</i> |
|------------------|---------------------------------------|--|--|
| Multiplication | $(f \cdot g)(x)$ $f(x) \cdot g(x)$ | $(f \cdot g)(x) = 6x(3x+2)$ $= 18x^2 + 12x$ | $(g \cdot f)(x) = (3x+2)6x$ $= 18x^2 + 12x$ |

Example 4: Let $f(x) = 4x$ and $g(x) = 8x$

A. $(f \cdot g)(x) =$

$$4x \cdot 8x = \boxed{32x^2}$$

B. $-2[g(x)] =$

$$-2(8x) = \boxed{-16x}$$

WHEN DO YOU PUT PARENTHESIS?

When the function has more than 1 term

Example 5: Let $f(x) = 4x + 1$, $g(x) = 2x$, $h(x) = 16x$, and $k(x) = 8$.

A. $(f \cdot g)(x) =$

B. $(g \cdot g)(x) =$

C. $(f \cdot k)(x) =$

D. $(f \cdot h)(x) =$

E. $(h \cdot g)(x) =$

F. $(h \cdot k)(x) =$

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| | | | |
|------------------|------------------|-----------------|-------------|
| Practice: | $f(x) = x - 8$ | $g(x) = 2x + 3$ | $h(x) = 3x$ |
| | $j(x) = x^2 + 5$ | $k(x) = 12x$ | |

A. $(f + g)(x) =$

B. $(g - f)(x) =$
 $\cancel{2x} + 5 - (x - 8) = 2x + 3 - x + 8$
 $\boxed{x + 11}$

C. $4[j(x)] =$

D. $(h \cdot g)(x) =$
 $6x^2 + 9x$

E. $(h - k)(x) =$

F. $6[g(x)] + 2 =$
 $|2x + 20|$

G. $2[g + k](x) =$

H. $(j - f)(x) + 8 =$
 $x^2 - x + 21$

I. $(f + f)(x) =$

J. $\left(\frac{g}{h}\right)(x) =$ 1